

# Meet 3 – Event A 2019-20

Questions are worth 2-2-2-4-4 points respectively. *No calculators allowed* 

- 1. What is the greatest common factor of 48 and 78?
  - **\_2.** Write the expression in simplest radical form.  $\sqrt{108}$

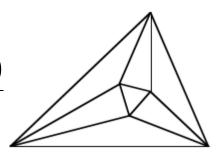
<u>*n*</u> = \_\_\_\_\_**3.** The equation shows  $\frac{1}{49}$  as the product of powers of 7.

$$\frac{1}{49} = 7^3 \times 7^{\gamma}$$

What value for *n* makes the equation true?

- <u>ft</u><sup>3</sup> **4.** Christy is helping to fill a tank with water. The tank is a rectangular prism that measures 8 feet wide, 11 feet long, and 6 feet deep. The tank is  $\frac{1}{3}$  full of water. How much more water, in cubic feet, should Christy add to fill the tank completely?
- <u>%</u> **5.** Haakon, Andrew, Elijah, and Rose shared a pizza.
  - Haakon ate 16% of the pizza.
  - Andrew ate 50% more of the pizza than Haakon ate.
  - Elijah ate 50% more of the pizza than Andrew ate.
  - Rose ate the rest of the pizza.

What percentage of the pizza did Rose eat?



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### Answers

Questions are worth 2-2-2-4-4 points respectively.

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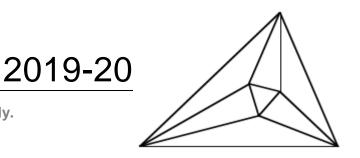
<u>6 $\sqrt{3}$ </u> **2.**  $\sqrt{108} = \sqrt{9 \times 12} = 3\sqrt{4 \times 3} = 6\sqrt{3}$ 

n = -5 3. 
$$\frac{1}{49} = \frac{1}{7^2} = 7^{-2}$$
  
 $7^{-2} = 7^{3+n} = 7^{3+(-5)}$ 

352 ft<sup>3</sup> **4.** 
$$8 \times 11 \times 6 = 528$$
  
528  $\times 2/3 = 352$ 

24% **5.** H: 0.16

A: 1.5(0.16) = 0.24 E: 1.5(0.24) = 0.36 R: 1 - (0.16 + 0.24 + 0.36) = 0.24 = **24%** 



Questions are worth 2-2-2-4-4 points respectively.

Meet 3 – Event B

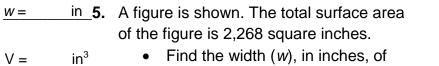
#### No calculators allowed

\_\_\_1. What is the least common multiple (LCM) of 16 and 20?

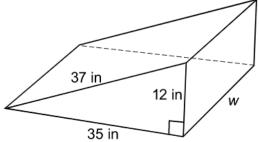
<u>x =</u> **2.** Solve for *x*. Write your answer as a reduced fraction.

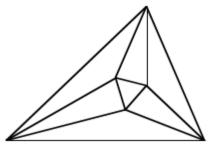
$$\frac{1}{4}(2x+8) = 1.5 + 4x$$

- **\_3.** Evaluate the expression when x = 2.  $(x^2 + 2x + x^3)^2 \cdot (x^4)^{-2}$
- <u>mm<sup>3</sup></u> **4.** A microscopic crystal is in the shape of a cube with an edge length of 8<sup>-5</sup> mm. What is the volume, in mm<sup>3</sup>, of the crystal? Write your answer in exponential form using only positive exponents.



- Find the width (*w*), in inches, of the figure.
- Find the volume (V), in cubic inches, of the figure.





#### Answers

Questions are worth 2-2-2-4-4 points respectively.

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x = 1/7 2. 
$$\frac{1}{4}(2x+8) = 1.5 + 4x; \frac{1}{2}x + 2 = \frac{3}{2} + 4x; \frac{1}{2} = \frac{7}{2}x; x = \frac{1}{7}$$

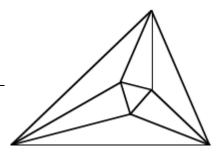
**1 3.** 
$$(x^2 + 2x + x^3)^2 \cdot (x^4)^{-2} = (4 + 4 + 8)^2 \cdot 16^{-2}$$
  
 $(16)^2 \cdot 16^{-2} = 16^0 = 1$ 

$$\underline{\frac{1}{8^{15}} \text{ mm}^3}_{4.} (8^{-5})^3 = 8^{-15} = \frac{1}{8^{15}}$$

w = 22 in 5. 
$$SA: 2\left(\frac{35\times12}{2}\right) + 35w + 12w + 37w = 2268$$
  
 $SA: 420 + 84w = 2268; 84w = 1848; w = 22$   
V = 4,620 in<sup>3</sup>  $V: \left(\frac{35\times12}{2}\right) \times 22 = 210 \times 22 = 4620$   
2 points per  
response

## Meet 3 – Team Event 2019-20

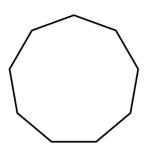
Questions are worth 4 points each. *No calculators allowed* 



- **1.** A cube is painted red and then cut into 27 congruent cubes. How many of these cubes are painted red on exactly one face?
- Elsa has had her bank account for 2 years. During the first year, the amount of money in her account increased by 200%. During the second year, it decreased by 25%. If her account currently contains \$450, what was the amount of her initial deposit?
  - **3.** Simplify. Use only positive exponents in your answer.

 $\frac{3x^{-7} \cdot 4x^0}{8x^3 \cdot x^{-2}}$ 

- **4.** There are 10,300 cm<sup>3</sup> of water in a cooler. Don completely fills cone-shaped cups with water from the cooler. Each cup has a radius of 3 cm and a height of 7 cm. What is the maximum number of cups Don can fill with the water from the cooler? Use  $\frac{22}{\pi}$  in your calculations for  $\pi$ .
  - **\_\_5.** Given  $a^{1/5} = b$ , what is the value of  $a^{2/5}$ ?
- 6. How many diagonals does the nonagon have?



**7.** Solve for *x*.  $-\frac{1}{3}(4-2x) = \frac{5}{2}x + 6$ 

*X* =

- <u>%</u>8. The speed of light is approximately  $3 \times 10^8$  meters per second. A comet is traveling at approximately  $6 \times 10^4$  meters per second. At what **percentage** of the speed of light is the comet traveling?
- **9.** Selma and Tran each have a bag of blueberries. Selma's bag has 96 blueberries, and Tran's bag has 128 blueberries. They each divide their blueberries into equal-sized groups. What is the greatest number of blueberries that could be in both Selma's and Tran's groups?
- \_\_\_\_\_**10.** Simplify:  $\sqrt{135x^6yz^5}$

### Meet 3 – Team Event 2019-20

### Answers

27

Questions are worth 4 points each.

- 6 1. Each face of the larger cube must have 9 congruent squares. Only the middle square will get painted on exactly one side. Since there are 6 faces, there are 6 such squares.
- **2.** x = initial deposit $x + 2x = 1^{st} year; 0.75(x + 2x) = 2^{nd} year$ 0.75(x + 2x) = 450; 0.75(3x) = 450; 2.25x = 450; x = 200

$$\underbrace{\frac{3}{2x^8}}_{8x^3} \mathbf{3.} \quad \frac{3x^{-7} \cdot 4x^0}{8x^3 \cdot x^{-2}} = \frac{3 \cdot 4 \cdot x^2}{x^7 \cdot 8x^3} = \frac{12x^2}{8x^{10}} = \frac{3}{2x^8}$$

**156 4.** Volume of each cup  $=\frac{1}{3}\pi r^2 h = \frac{1}{3}\pi (9)(7) = 21\pi = 21\left(\frac{22}{7}\right) = 66$ 10300 ÷ 66 = 156.  $\overline{06} \rightarrow \text{Max cups} = 156$ 

b<sup>2</sup> **5.** 
$$a^{1/5} \cdot a^{1/5} = a^{(1/5+1/5)} = a^{2/5}; \ b \cdot b = b^2$$

**6.** From each vertex, 6 diagonals can be drawn. There are 9 vertices, so there are 54 possible diagonals. However, this number needs to be cut in half to avoid duplicating diagonals. (For instance, a diagonal drawn from vertex 1 to vertex 5 is the same as the diagonal drawn from vertex 5 to vertex 1.)

$$\begin{array}{ccc} x = -4 & & \mathbf{7.} & -\frac{1}{3}(4-2x) = \frac{5}{2}x + 6; \ -\frac{4}{3} + \frac{2}{3}x = \frac{5}{2}x + 6; \ \left(\frac{2}{3} - \frac{5}{2}\right)x = 6 + \frac{4}{3}; \ \left(\frac{4}{6} - \frac{15}{6}\right)x = \frac{18}{3} + \frac{4}{3}; \\ & \left(\frac{4}{6} - \frac{15}{6}\right)x = \frac{18}{3} + \frac{4}{3}; \ -\frac{11}{6}x = \frac{44}{6}; \ x = -4 \\ \hline & \mathbf{0.02\%} & \mathbf{8.} & \frac{6 \times 10^4}{3 \times 10^8} = \frac{p}{100}; \ 600 \times 10^4 = (3 \times 10^8)p; \ \frac{6 \times 10^6}{3 \times 10^8} = p; \\ & 2 \times 10^{-2} = p; \ \mathbf{0.02} = p \end{array}$$

<u>32</u> **9.** GCF(96, 128) = **32** 

$$3x^{3}z^{2}\sqrt{15yz}$$
**10.**  $\sqrt{135x^{6}yz^{5}} = \sqrt{9 \cdot 15 \cdot (x^{2})^{3} \cdot y \cdot (z^{2})^{2} \cdot z} = 3x^{3}z^{2}\sqrt{15yz}$ 

